Multi-path 2-Port Channel Characterization for Galvanic Coupled Intra-body Communication

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ABSTRACT
Sensors implanted inside a body compose so called intra body networks (IBNs), which promise high degree of mobility, remote diagnostic accuracy, and the potential of directly activating the action of drug delivery actuators. To enable communication among these implanted sensors, we use the concept of galvanic coupling, in which extremely low energy electrical signals are coupled into the human body tissues by leveraging the conductive properties of the tissues. Several challenges emerge in this new communication paradigm, such as how to appropriately model the signal propagation through various tissue paths such as from muscle to skin across different tissue boundaries and quantify the achievable data rates. The main contributions in this paper are: (i) we build a 2-port tissue equivalent circuit model to characterize the body channel and to identify the range of suitable operating frequencies and (ii) we theoretically estimate the channel capacity for various sensor locations that incorporates factors like the tissue propagation path, operating frequency and noise level.

1. INTRODUCTION
Intra-body networks (IBNs) will revolutionize healthcare by allowing direct communication between implanted sensors and actuators through the body tissues. As conventional over the air radio frequency (RF) waves are strongly attenuated within the body, there is a growing concern for realizing energy-efficient transmissions within tissues. The advent of seamless, miniaturized nano-scale or MEMS-based sensors indicates possibilities for implanting several nodes that form a connected data network, apart from performing sensing and drug actuation roles. Among the candidate techniques for establishing IBNs, such as RF based, inductive coupling, capacitive coupling, and ultra-sound, we use galvanic coupling (GC). In GC-based communication, a pair of electrodes directly couple weak electric signals to the tissues in the order of 0.5 mW. The induced magnetic field is well below 2 mA/m, the permissible limit within the body [3]. Majority of the induced current coupled to the body passes through the return path of transmitter. A part of coupled signal propagates through the body and reaches the receiver electrodes (refer dashed arrow in Fig. 1(a)). The difference in voltage is detected by a corresponding pair of receiver electrodes that belong to another implant. Apart from being energy efficient when compared to RF, the communication in this scenario is less impacted by external environmental influence. In addition, GC operates with cost-effective transceivers and provides continuous real time connectivity. in terms of various network parameters. The state of the art in GC based IBNs (GC-IBN) [8, 1, 6] has been limited to on-surface communication, similar to node B to sink A communication in Fig. 1.(c). The channel behavior for implantable electrodes is obtained using a numerical model and a liquid (homogeneous) phantom reflecting typical muscle properties, but only at 27 MHz. However, to the best of our knowledge there is no work that studies the scenarios of signal propagation across tissues (Eg. from D to A in Fig. 1.(c)), demanding a three dimensional tissue structure modeling and characterizing the transverse path
from one tissue to other like the one presented here. In this paper, we thoroughly explore the propagation of GC signals through various tissue paths, such as over the skin, from skin to muscle or muscle to skin and through the muscle layer, which reveal important insights on the network size, link distance and capacity of GC-IBNs. The simple transfer function derived allows quick and accurate channel modeling over a wide range of frequency. The main contributions of this paper are as follows:

1. We determine the channel gain for various tissue paths using a 2-port tissue equivalent circuit model for wireless communication through the dry skin surface and inner tissue-layers of the human arm. Our theoretical approach is validated with previously conducted experiments for on-skin cases. We provide insights on suitable implant positions inside the body tissues, operating frequency offering better channel characteristics.

2. We formulate closed form expressions for the noise that impacts correct signal reception in GC-IBN and then estimate the signal to noise ratio, which is the first step towards selection of suitable modulation schemes.

3. We then estimate the capacity of a GC link and analyze the maximum traffic that can be accommodated in GC-IBN in terms of the number of nodes.

The rest of the paper is organized as follows. We derive the 2-port equivalent circuit models of the human arm in Section 2. An approximation of possible noise in GC-IBN with SNR and capacity formulations are given in Section 3. The channel characteristics obtained using the 2-port model are discussed in Section 4, for different tissue paths, distances and frequencies. Finally, Section 5 concludes the paper.

2. 2-PORT CIRCUIT MODEL

Individual tissues are represented as black-boxes in a 2-port model, constructed from the electrical properties of tissues that is configurable with tissue dimensions corresponding to a specific human subject. The principle benefit of this 2-port model is a simple first-approximation for the voltages and currents that are likely to be observed within the given tissue layer during communication. The black-box approximation makes it easier to add, remove or modify tissue dimensions within the model which otherwise is complicated and time consuming to alter the model appropriately for different parts of the body. The model works for signal propagation within the same tissue layer, adapts easily for different combinations of tissues, and describes the signal propagation through tissues from the input to output ports for a given choice of input frequency, transmitter-receiver distance (D), terminal separation (E) (refer Fig. 1(a)) and tissue thickness (T). As an added advantage, the port parameters enable direct observation of the scattering parameters at the electrode-tissue and tissue-tissue boundaries to assess the reflection and propagation at interfaces.

Tissue Impedance.

When live tissue cells are excited by an electrical signal, each cell activates its neighbor, enabling signal propagation through different paths. The cell membrane gives a capacitance effect allowing only the high frequency signal to pass through while the low frequency signal takes the extracellular path. Therefore, a biological cell can be modeled as parallel combination of resistance $R_{ext}$ (dissipation loss), and a combination of capacitor $C_m$ and intra-cellular resistance $R_{int}$, as given in Fig. 2(b). The R and C values can be completely described in terms of conductivity ($\sigma$) and relative permittivity ($\epsilon$) using Cole-Cole model [2]. The tissue admittance using RC elements can be calculated as,

$$Y = F_W \left( \frac{\sigma M_1}{\sigma M_1 + j \omega \epsilon M_2} \right)$$

where $M_1$ is the ratio of cross sectional area (A) and length of the channel (L) decided by the direction of impedance measurement, while $M_2$ is the ratio of A and thickness of channel, $F_W \in [1, 10]$ is the correction factor accounting for
variation in tissue water distributions. \( \kappa \) is the ratio of external to internal cell resistance. The tissue properties can be estimated without actual measurement such as tissue thickness approximation using BMI or triceps skin fold thickness.

**Single Tissue Equivalent Circuit.**

The 2-port equivalent of a single GC-coupled tissue is modeled using tissue impedance along the four propagation paths P1, P2, P3 (Fig. 2(a)) and P4 (Fig. 2(c)) taken by the injected current that are obtained as follows.

- **P1** is the primary return path offering the direct impedance \( Z_D \) that channels the majority of current from the terminal to reference electrodes in the transmitter. In this case \( M_1 \) given in (1) takes the form \((E_L \times T)/E_S \), where \( E_L \) is a side of the square electrode, T is tissue thickness and \( E_S \) is the terminal-reference electrodes separation in transmitter/receiver.

- **P2** serves as a pathway for a portion of current directed towards the receiver electrodes through longitudinal impedance \( Z_L \) between the transmitter and receiver electrodes. \( M_2 \) of \( Z_L \) is calculated as \((E_L \times T)/D \), where, \( D \) is the transmitter-receiver separation distance.

- **P3** is the current propagation path from source terminal in transmitter to the reference terminal in receiver through cross impedance \( Z_C \). Here, \( M_1 \) becomes \((\sqrt{2}E_L \times T)/\sqrt{D^2 + E_S^2} \). In all the above cases, \( M_2 \) is chosen to be the tissue thickness.

- **P4** is the current propagation path to adjacent tissue layer through transverse impedance \( Z_T \). To compute this impedance, \( M_1 \) is substituted with \( T/A_e \), where, \( A_e \) is the electrode area. In this case, \( M_2 \) is assigned the value of \( E_S \).

The coupling impedance offered by the electrode-tissue interface determines the amount of signal entering into the tissue. This impedance, denoted as \( Z_{C_T} \) (refer Fig. 2(a)), is a function of frequency, area of contact, tissue hydration, electrode material and surface treatment and is modeled similar to the approach in [5] as

\[
R_{C_T} = \rho_C \omega f^{m} / A_e
\]

\[
X_{C_T} = 1/j \omega C_T = K_1 \epsilon_{C_T} \omega f^{m} / A_e
\]

where, \( f \) is the frequency of operation, \( \rho_C \) is the electrode and hydrogel resistivity, \( A_e \) is electrode area, \( K_1 \in (0,1) \) is chosen based on the tissue hydration, \( \epsilon_{C_T} \) depends on electrode permittivity, and \( m \) is the constant for activation control. The dots in Fig.2(a) represents the possibility of attaching \( Z_{C_T} \) to any tissue based on the tissue path under study. For instance, in the skin to muscle path, the coupling impedance is included in input impedance of skin and output impedance of muscle. Using the impedance defined above, the 2-port equivalent of a tissue can be defined in terms of \( Z \)-parameters represented as a \( 2 \times 2 \) matrix of complex numbers that obeys the relation, \( [V'] = [Z'][I] \) where \([V'] = [V_1 V_2] \) is the voltage vector, and \([I'] = [I_1 I_2] \) is the current vector at the input and output ports. The \( Z \) parameter of each tissue can be calculated as,

\[
[Z] = \begin{bmatrix}
Z_{11} & Z_{12} \\
Z_{21} & Z_{22}
\end{bmatrix} = \begin{bmatrix}
2Z_LZ_T & Z_T \\
Z_T & Z_L + 2Z_T
\end{bmatrix}
\]

with \( Z_1 = \frac{2Z_L Z_T}{Z_T - Z_L} \) and \( Z_2 = \frac{Z_T Z_D}{Z_T + Z_D} \). For the tissue layer receiving signal from another layer, \( Z_1 \) becomes \( \frac{2Z_L Z_T}{Z_T - Z_L} (1 + Z_T) \), where \( Z_T \) is the transverse impedance offered by the interface between tissue layers. Similar to impedance parameters, we also use admittance parameters \( [Y] \) for handling parallel impedance and ABCD parameters \( [A] \) for handling cascaded impedance.

### 2.1 Human Arm Equivalent 2-port Network

We approximate the galvanic coupled human arm as layered dielectric block of tissues as given in Fig. 2.(c). The model of 700 mm length has four tissue layers - outer dry skin, fat, muscle and cortical bone (hard outer covering of bone) of thickness 1 mm, 9 mm, 25 mm and 20 mm respectively. For developing a tractable model, we assume uniform tissue dimensions along the paths indicated by \( \bigotimes \) and \( \otimes \) in Fig. 2(a). However, it is possible to introduce asymmetry in the model by varying the electrodes separation \( E_S \), and/or \( T \) at transmitter and receiver.

In the following multi-layer discussion the superscript \( i \) and \( j \) denote a specific tissue layer, i.e., \( i,j \in (S,F,M,B) \), with the substitutions of \( S \) for skin, \( F \) for fat, \( M \) for muscle, and \( B \) for bone. The single tissue impedance \( Z_D \) and \( Z_L \) in Fig. 2.(a) become \( Z_{D_i}^{-1} \) and \( Z_{L_i}^{-1} (i \in \{S,F,M,B\}) \) denoting path from layer \( i \) to \( j \). The transmitter electrodes, attached on the tissue, form the in port, and the receiver electrodes form the out port. This concept is clarified further with a sample case of the transmitter and receiver coupling locations on skin to muscle path (S-M path) is shown in Fig. 2.(c). Figure 3 illustrates the location of coupling electrodes when on-surface nodes are moved into muscle tissue. We explain the development of the analytical models for skin to skin (S-S), muscle to muscle (M-M), skin to muscle (S-M) and muscle to skin (M-S) tissue paths of signal propagation next. We ignore the paths through fat and bone tissues as the implants are not commonly placed in these tissues.

- **S-S path model** Here, the transmitter and receiver sensor electrodes are positioned on the skin surface with coupling impedance \( Z_{C_S} \). The current flow is through skin, and through the parallel paths in fat, muscle and bone layers. The input impedance of the fat layer includes the transverse impedance from skin as the signal originates in skin. Similarly, the input impedance of muscle and bone layers include the transverse impedance from the fat and muscle tissues, respectively. The overall admittance is:

\[
[Y^{S-S}] = [Y^{S}] + [Y^{F}] + [Y^{M}] + [Y^{B}] \tag{2}
\]

- **M-M path model** To study the channel response at the muscle layer, the transmitter and receiver sensor electrodes are moved inside muscle tissue (M-M path), in which the dominant path of the current also lies. Along the M-M path, the muscle tissue is in parallel to that of skin and fat tissues and with the bone. In this case, the input impedance of
fat and bone layers include the transverse impedance from the muscle layer as the signal originates from the muscle. The input impedance of skin layer includes the transverse impedance of muscle and fat tissues. The total channel admittance at M-M path can be calculated as the parallel combination of individual tissues as given in S-S path model.

**• S-M path model** When the transmitter is on skin and the receiver is in muscle, the impedance offered by the S-M path is measured as the cascaded skin-fat-muscle ports that is in parallel to that of bone. The transverse impedance is calculated as in the S-S case as the signal source is at skin. Assuming $A^S$, $A^F$ and $A^M$ as the $[A]$ parameters of skin, fat and muscle, the combined $[A]$ parameter for the cascaded skin-fat-muscle tissues is given by


With the added parallel effect of bone tissue, the overall admittance of the S-M path is computed as follows.

$$[Y]^{S-M} = \begin{bmatrix}
\frac{A^{S,F,M}}{A^{S,F,M}} & -\Delta[A^{S,F,M}] \\
\frac{A^{S,F,M}}{A^{S,F,M}} & 1 \\
\end{bmatrix} + [Y^B]$$  \(4\)

**• M-S path model** For the M-S path, with the source at muscle, the transverse impedance is calculated as in M-M path. Here, the ABCD parameter of cascaded muscle, fat and skin tissues is given by


The admittance parameter of M-S path is obtained by computing the cascaded muscle, fat and skin tissue in parallel to the bone. The resulting expression is similar to the computation in (4). The voltage gain $G(w, E_L, D, E_S, [T])$ can be calculated from the total equivalent $Z$ parameters (inverse of $Y$ parameter matrix) $[Z^{-1}]$ as,

$$\frac{V_{out}}{V_{in}} = \frac{Z_{Load}^{i-j}}{(Z_{11}^{i-j} + Z_{CA})(Z_{22}^{i-j} + Z_{Load}) - Z_{21}^{i-j} Z_{12}^{i-j}}$$  \(6\)

where $i,j \in \{S,M\}$ for denoting S-S, S-M, M-S and M-M paths individually. The gains along the four paths above is plotted in Fig. 5 and analyzed in section 4.

### 3. NOISE, SNR & CAPACITY ESTIMATION

To fully determine the ability of the receiver to decode the signal and determine the achievable data rate, the estimation of noise is of critical importance. Once this noise level is known, the signal to noise ratio (SNR) can be computed, and the impact of various modulation schemes can be studied. To quantify the noise level, we focus on a single pair of transmitter-receiver nodes. We model the noise by approximating the power spectral densities (p.s.d) of thermal noise, electrode coupling noise and RF radiation interference as described below.

**Thermal Noise $N_T$:** The thermal noise depends mainly on frequency and temperature and can be calculated as:

$$N_T(f) = \sqrt{4kTR} \frac{W}{\sqrt{Hz}}$$  \(7\)

where $T$ is the absolute temperature in Kelvin, $k$ is Boltzmann constant, and $R$ is electrode and tissue resistance.

**Electrode coupling noise $N_E(f)$:** This noise occurs at the interface where the electrode is attached to the tissue. The skin-electrode interface noise can be related to the real part of the skin-electrode impedance, and is equivalent to the thermal noise at high frequencies. We use the noise p.s.d of surface electrodes as approximated in [4] as:

$$N_E(f) = 1/f^\alpha, 1.5 < \alpha < 2.0$$  \(8\)

where $\alpha$ is a correction factor that depends on the gel type and skin properties.

**RF Radiation interference $I_{rad}$:** RF radiation from sources including TV and radio broadcast signals, transmissions in the so called lost band (160 – 190 KHz) and amateur radio (135.7 – 137.8 KHz) that are in 100 KHz to 1 MHz range might be a potential source of interference. We approximate these interference sources as Additive White Gaussian Noise with IID Gaussian random variable $N(0, \varphi)$ of zero-mean and variance $\varphi$.

The channel’s Signal to Noise Ratio (SNR) can be calculated as

$$SNR^{i-j} = \frac{P_t \cdot G^{i-j}(w, E_L, D, E_S, [T])}{(N_T + N_E + I_{rad}) \Delta f}$$  \(9\)

where $P_t$ is the transmitter power and $\Delta f$ is the receiver bandwidth. The SNR estimated can be used to calculate bit error rate (BER) for a given modulation type, $f$ and $D$. We term the maximum distance of communication between the transmitter and receiver beyond which the BER exceeds the desired value as the threshold distance $D_{Th}$. For a node to communicate with sink at a distance $D > D_{Th}$, (say from a node implanted at wrist to sink on shoulder), multi-hop...
Table 1: Gain, Capacity and BER for BPSK Modulation at $\varphi = 1e8$

<table>
<thead>
<tr>
<th>Distance (cm)</th>
<th>Frequency (KHz)</th>
<th>Gain (dB)</th>
<th>Channel Capacity (bps)</th>
<th>BER (BPSK)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>S-S</td>
<td>M-S</td>
<td>M-M</td>
</tr>
<tr>
<td>10</td>
<td>100</td>
<td>-37</td>
<td>-30.5</td>
<td>-18</td>
</tr>
<tr>
<td>10</td>
<td>1000</td>
<td>-38</td>
<td>-38.5</td>
<td>-16.8</td>
</tr>
<tr>
<td>20</td>
<td>100</td>
<td>-52</td>
<td>-47</td>
<td>-31</td>
</tr>
<tr>
<td>20</td>
<td>1000</td>
<td>-53</td>
<td>-55</td>
<td>-29.7</td>
</tr>
</tbody>
</table>

Figure 5: (a) Gain at 4 paths ($D = 15 cm$, $E_L = 1 cm$, & $E_S = 5 cm$)

paths using relays are required. We assume that a relay could connect a number of nodes in single hop arranged in a star topology. Each relay in-turn could be connected to the sink via multi-hop links. When a spanning tree is constructed that connects all the nodes in an upper limb to a sink through relays as illustrated in Fig. 4, it results in the formation of a bottleneck link. This link carries the entire upper limb traffic to the sink that we call as the last hop link (LH), (refer Fig. 4). The capacity of LH link, $C(LH)$, for various lengths and paths of LH using Shannon - Hartley theorem, can be determined as

$$C(LH) = W \log_2(1 + SNR^{i-j}) \ [\text{bits/s}], \forall i, j \in \{S, M\}$$

where $W$ is transmission bandwidth. According to Max-flow Min-cut theorem, a minimum cut on LH, with maximum capacity $C(LH)$, limits the maximum number of nodes in the sub-network and the maximum possible data rate at each node [7].

For reliable communication to and from the upper limb GC-IBN, the total traffic through LH should be less than $C(LH)$. Consequently, for the $N$ nodes in upper limb sub-tree to communicate reliably, the following condition has to be satisfied.

$$\sum_u R(u) < C(LH), \forall u \in \{1, ..., N\}$$  \hspace{1cm} (10)

where $R(u)$ is the total data rate to and from node $u$. Assuming equal data rate $\bar{R}$ in all the $N$ nodes, the maximum possible $N$ in subnetwork, $N_{Max}$, is limited by

$$N_{Max} < \frac{C(LH)}{\bar{R}}$$  \hspace{1cm} (11)

4. RESULTS AND DISCUSSIONS

The channel gain obtained for the four paths obtained using the 2-port model derived in Sec.2 at $D = 15 cm$, $E_S = 5 cm$, and $E_L = 1 cm$ are given in Fig. 5. The gain along the S-S path has a peak at 500 KHz and decreases beyond 1MHz.

- **Results verification using literature**: The clinical trial results in [8] match exactly with our analytical results as the measurement set-up is similar to our model assumptions presented above. However, though our results matches closely with the other literature measurement at 100 KHz as shown in Fig.6, there is a difference of approximately 7 dB and 3 dB with [1] and [6] respectively at 1 MHz.

The difference in gain in the latter two cases are likely due to the variations in the electrode dimensions, electrode material, physical tissue dimensions in the measurement set-ups. For instance, in [6], the skin thickness was assumed to be 1.5 mm with $E_S = 80 mm$ while we assigned them 1 mm and 100 mm respectively. Similarly, in [1], the radius of the subject’s arm is 47.5 mm, which we modeled as 55 mm. There are other inherent measurement uncertainties including surface treatment at electrode attachment, tissue temperature and hydration levels that we model using parameters $F_{W}$ and $Z_{C_o}$ and are not specified in the corresponding literature. Also, the conductivity and permittivity of tissues also vary among individuals by +/- 0.1 S/m and +/- 0.05 S/m in the range of frequency used [9] that contribute to the difference between our results and the results in [1] and [6]. In order to overcome other measurement uncertainties in GC-IBN, an adaptive communication system is required that alters the transmission parameters based on the time dependent estimation of channel characteristics. For instance, estimating bounds on interference and allowing sufficient tol-
5. CONCLUSIONS

The channel gain calculations, the achievable range of communication, BER and link capacities analyzed in this paper demonstrates GC-IBN as a feasible candidate for network implanted body nodes. Our 2-port model helps in quick characterization of the channel within the body. We have derived the expressions for noise and data rates that are feasible in such networks and future work will be focused on higher layer networking design.

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6. REFERENCES